

EXpérimenter des Problèmes de Recherche Innovants en Mathématiques à l'Ecole

The experiment al dimension in mathematical research problems

Gilles Aldon Viviane Durand-Guerrier

The context of the research Questions The school

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example 1 example 2

Presentation of the resource The experimental dimension in mathematical research problems

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INRP, équipe maths LEPS, Université de Lyon EXpérimenter Problèmes Recherche Innovants Mathématiques Ecole

July 13, 2007



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Presentation of the resource

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- Jean DERUAZ, professeur en lycée, (IREM)
- Thierry DIAS, Université Lyon 1 (LEPS, IUFM)
- Viviane DURAND-GUERRIER, didacticienne, Université Lyon 1 (LEPS, IUFM, IREM)
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- Claire TARDY, formatrice d'enseignants (IREM,IUFM)



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Presentation of the resource

Theoretical references :

- theory of situations of Brousseau
- mathematics
- the place of the mathematical objects (Quine, Frege, Gardies)

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Presentation of the resource "In a mountain hike one needs a goal, but the main interest of hiking is not the goal but the walk" Jean-Yves Girard (2007)

Using "research problems" in the classroom in order to develop exclentific methods:

heuristics

soning

They can, also give sense to some concepts and make the learners construct mathematical notions by themseives

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Presentation of the resource

1 starting with "classical" research problems;

- studying the mathematical concepts possibly taught through the resolution of the problem;
- going from a mathematical situation to a situation for the students;

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If focusing on the experimental dimensions in problem solving



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Presentation of the resource 1 starting with "classical" research problems;

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- 3 going from a mathematical situation to a situation for the students;

If focusing on the experimental dimensions in problem solving



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Presentation of the resource 1 starting with "classical" research problems;

- 2 studying the mathematical concepts possibly taught through the resolution of the problem;
- **3** going from a mathematical situation to a situation for the students;

 focusing on the experimental dimensions in problem solving



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Presentation of the resource **1** starting with "classical" research problems;

- 2 studying the mathematical concepts possibly taught through the resolution of the problem;
- **3** going from a mathematical situation to a situation for the students;

4 focusing on the experimental dimensions in problem solving



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Presentation of the resource

Elaborating problems or fields of problems

- linked with mathematical concepts
- allowing the students to shuttle between the experimental part of the research and the structured construction of mathematical knowledge

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Presentation of the resource develop specific tools allowing us to understand and to analyse how the mathematical web is spun all around the objects which are mobilised in the problem solving

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Presentation of the resource The results are based on observations experienced in classrooms with pupils and students between secondary school and university

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The experimental part of mathematics

Three examples

To break down 1 into the sum of fractions of numerator 1.



Can you find two distinct integers a et b such as: $1 = \frac{1}{a} + \frac{1}{b}$? Can you find three distinct integers a, b and c such as: $1 = \frac{1}{a} + \frac{1}{b} + \frac{1}{c}$? Can you find four distinct integers a, b, c and d such as: $1 = \frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{a}$? Continue...

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The experimental part of mathematics

Three examples

Regions inside the circle



To find the maximum number of regions inside a circle by joining n points of a circle;

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Presentation of the resource Polya urns.



Three examples

An urn contains two balls: a white one and a black one. At each time a ball is drawn from the urn. The contents of the urn are then altered, puting one more ball in the urn of the same color of the drawn ball. Study the dynamic of the urn.



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Presentation of the resource Solving problems: linking a mathematical situation with our own knowledge (Dias, 2005)

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Presentation of the resource Our experiment field is constructed on our personal knowledge, on familiar objects and uses, more or less, familiar tools (particularly true for technological tools)

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Presentation of the resource

- $\frac{1}{a} + \frac{1}{b} = 1$ hence a b = ab
- no a + b = ab
- then -a b = -ab
- we have made a great headway! (laugh)
- I hope we are not going to have something like that in our next assessment!



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Presentation of the resource V : The smallest fraction with integers is one half; you can't have a smaller one.

: 1 isn't possible, the smallest fraction is $\frac{1}{2}$.

: Can you explain?

V: For the second question: a = 2, b = 3, c = 6 for the third question: 3 a = 2, b = 3, c = 9, d = 18

R : Why is the first question impossible?

(: Write the first (fractions with numerator 1)

R : And why is it impossible?

(: In any case, a must be 2

R : Perhaps, is there an other fraction with a numerator 1 which gives 0.5...

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Presentation of the resource Experiments allow us to conjecture but also to **refute** conjectures;

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Presentation of the resource

$$nb_n = 1 + \left(\begin{array}{c}n\\2\end{array}\right) + \left(\begin{array}{c}n\\4\end{array}\right)$$

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example 1 example 2

Presentation of the resource It's also possible to do an experiment in the field of the graph theory

Completing the graph in order to make it planar



Hence we have to count:

the vertices :

the edges:

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example 1 example 2

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 $n + \left(\begin{array}{c} n\\ 4 \end{array}\right)$

 $n + \begin{pmatrix} n \\ 2 \end{pmatrix} + 2 \begin{pmatrix} n \\ a & b \end{pmatrix} + 2 \begin{pmatrix} n \\ a & b & b \end{pmatrix} = 2$

the edges :



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Presentation of the resource Using the Euler's formula :

F=E-V+2

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Presentation of the resource Using the Euler's formula :

$$F = n + \left(\begin{array}{c}n\\2\end{array}\right) + 2 \left(\begin{array}{c}n\\4\end{array}\right) - n - \left(\begin{array}{c}n\\4\end{array}\right) + 2$$

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Presentation of the resource

Using the Euler's formula :

$$F = \left(\begin{array}{c} n\\4 \end{array}\right) + \left(\begin{array}{c} n\\2 \end{array}\right) + 2$$

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Presentation of the resource Using the Euler's formula :

Hence, the number of inside faces is:

$$F = \left(egin{array}{c} n \\ 4 \end{array}
ight) + \left(egin{array}{c} n \\ 2 \end{array}
ight) + 1$$

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Egyptian fractions

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Presentation of the resource

A difficulty is to transform a productive mathematical situation into a productive didactical situation

"Setting up a real experimental approach, in which the different steps are not bypassed needs appropriate situations and a demanding didactical management" Michèle Artigue, 2007



Egyptian fractions

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Presentation of the resource

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Presentation of the resource

The aim of our work consists in suggesting class organisations linked with didactical variables of the mathematical situation





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Polya's urn

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Presentation of the resource

An urn contains two balls: a white one and a black one. At each time a ball is drawn from the urn. The contents of the urn are then altered, puting one more ball in the urn of the same color of the drawn ball. Study the contents of the urn.

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Polya's urn

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Polya's urn

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Presentation of the resource

The experiments are local;

 Institutionalization has to take into account the different approaches;

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The mathematical analysis helps to understand these different approaches.



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Presentation of the resource

- The experiments are local;
- Institutionalization has to take into account the different approaches;

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The mathematical analysis helps to understand these different approaches.



The experiment al dimension in mathematical research problems

Gilles Aldon Viviane Durand-Guerrier

The context of the research

The school context

The experimental part of maths example 1 example 2

Presentation of the resource

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The context o the research Questions

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"Are you sure there is a real law" Student bac+1

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